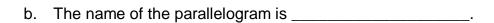
## **Notes: PARALLELOGRAMS**

<u>Content Objective:</u> I will be able to apply properties of parallelograms to determine the measures of sides, diagonals, and/or angles.

| TERM          | DESCRIPTION   | EXAMPLE |
|---------------|---|---------|
| QUADRILATERAL | A closed figure formed by segments intersecting at their endpoints. |         |
| PARALLELOGRAM | A quadrilateral in which opposite sides are                         |         |
| DIAGONAL      | Segment joining vertices in a polygon                               |         |

**EXAMPLE 1:** Refer to the figure on the right to identify or name each of the following:

a. The four vertices are \_\_\_\_\_



c. The opposite sides are \_\_\_\_\_\_.



- e. The consecutive angles are \_\_\_\_\_\_.
- f. The diagonals are \_\_\_\_\_.

Label the figure to represent each of the properties listed below:

## **PROPERTIES OF PARALLELOGRAMS**

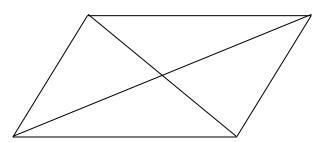
1. Opposite sides are \_\_\_\_\_\_ slope.

2. Opposite sides are \_\_\_\_\_\_.

3. Opposite angles are \_\_\_\_\_\_.

4. Consecutive angles are \_\_\_\_\_...

5. Diagonals \_\_\_\_\_ each other.

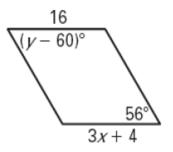


For Example #2, draw and label each parallelogram described then determine the value of x.

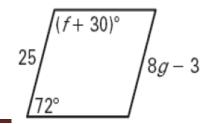
**EXAMPLE 2:** If **ABCD** is a parallelogram,  $\mathbf{m} \angle \mathbf{A} = \mathbf{X}^{\circ}$  and  $\mathbf{m} \angle \mathbf{D} = (2\mathbf{X} - 3)^{\circ}$ .

QUICK CHECK: If ABCD is a parallelogram,  $m\angle D = X^{\circ}$  and  $m\angle A = (3x + 4)^{\circ}$ .

**EXAMPLE 3:** Use the parallelogram to find the indicated values.



QUICK CHECK: Use the parallelogram to find the indicated values.

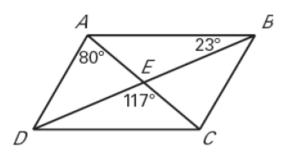


For Example # 4, draw and label each parallelogram described then determine the value of x.

**EXAMPLE 4:** XYZW is a parallelogram with diagonals  $\overline{XZ}$  and  $\overline{YW}$  that intersect at point A. If XA = 3m and ZA = 5m - 4, find m.

**QUICK CHECK:** XYZW is a parallelogram with diagonals  $\overline{XZ}$  and  $\overline{YW}$  that intersect at point A. If YA = 2t and WA = 3t - 4, find YA.

**EXAMPLE 5:** Use parallelogram ABCD to find the indicated values.



$$m \angle AEB = \underline{\hspace{1cm}}^{\circ}$$

$$m \angle BAD = \underline{\hspace{1cm}}^{\circ}$$

$$m \angle BAE = \_\_\_^{\circ}$$

$$m \angle DCE = \_\_\_$$
°

$$m \angle AED = \underline{\hspace{1cm}}^{\circ}$$

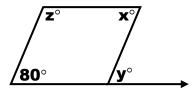
$$m \angle ADC = \underline{\hspace{1cm}}^{\circ}$$

$$m \angle ECB = \underline{\hspace{1cm}}^{\circ}$$

$$m \angle DCB = \underline{\hspace{1cm}}^{\circ}$$

## **EXAMPLE 6:** For each parallelogram, find the values of x, y, and z.

a.

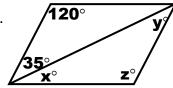


X = \_\_\_\_\_

y = \_\_\_\_\_

z = \_\_\_\_\_

b.

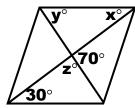


X = \_\_\_\_\_

y = \_\_\_\_\_

z = \_\_\_\_\_

c.



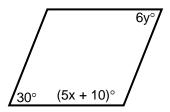
x = \_\_\_\_\_

y = \_\_\_\_\_

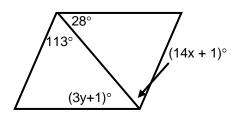
z = \_\_\_\_

**QUICK CHECK:** Find the values of  $\mathbf{x}$  and  $\mathbf{y}$  to ensure that each quadrilateral is a parallelogram.

a.



b.



x = \_\_\_\_\_

y = \_\_\_\_\_

x = \_\_\_\_\_

y = \_\_\_\_\_