## Notes: PARALLELOGRAMS

Content Objective: I will be able to apply properties of parallelograms to determine the measures of sides, diagonals, and/or angles.

| TERM | DESCRIPTION | EXAMPLE |
| :---: | :--- | :---: |
| QUADRILATERAL | A closed figure formed by <br> intersecting at their endpoints. |  |
| PARALLELOGRAM | A quadrilateral in which opposite <br> sides are |  |
| DIAGONAL | Segment joining <br> vertices in a polygon |  |

EXAMPLE 1: Refer to the figure on the right to identify or name each of the following:
a. The four vertices are $\qquad$ .
b. The name of the parallelogram is $\qquad$ .
c. The opposite sides are $\qquad$ -

d. The opposite angles are $\qquad$ .
e. The consecutive angles are $\qquad$ .
f. The diagonals are $\qquad$ .

Label the figure to represent each of the properties listed below:

## PROPERTIES OF PARALLELOGRAMS

1. Opposite sides are $\qquad$ therefore they have the $\qquad$ slope.
2. Opposite sides are $\qquad$ .
3. Opposite angles are $\qquad$ .
4. Consecutive angles are $\qquad$ ..
5. Diagonals $\qquad$ each other.


-     -         -             -                 -                     -                         -                             -                                 -                                     -                                         -                                             -                                                 -                                                     -                                                         -                                                             -                                                                 -                                                                     -                                                                         -                                                                             -                                                                                 - 

For Example \# 2, draw and label each parallelogram described then determine the value of $x$.
EXAMPLE 2: If $\boldsymbol{A B C D}$ is a parallelogram, $\boldsymbol{m} \angle \boldsymbol{A}=x^{\circ}$ and $\boldsymbol{m} \angle \boldsymbol{D}=(2 x-3)^{\circ}$.

$$
x=
$$

$\qquad$
QUICK CHECK: If $\boldsymbol{A B C D}$ is a parallelogram, $\boldsymbol{m} \angle \boldsymbol{D}=x^{\circ}$ and $\boldsymbol{m} \angle \boldsymbol{A}=(3 x+4)^{\circ}$.

$$
x=
$$

$\qquad$

EXAMPLE 3: Use the parallelogram to find the indicated values.

QUICK CHECK: Use the parallelogram to find the indicated values.

$$
\begin{aligned}
& f= \\
& g=
\end{aligned}
$$

$\qquad$
y = $\qquad$


For Example \＃4，draw and label each parallelogram described then determine the value of $x$ ．
EXAMPLE 4：XYZW is a parallelogram with diagonals $\overline{X Z}$ and $\overline{\boldsymbol{Y W}}$ that intersect at point $\boldsymbol{A}$ ． If $X \mathbf{X A}=3 m$ and $\mathbf{Z A}=5 m-4$ ，find $\boldsymbol{m}$ ．
$\mathrm{m}=$ $\qquad$

QUICK CHECK：XYZW is a parallelogram with diagonals $\overline{X Z}$ and $\overline{\boldsymbol{Y} W}$ that intersect at point $\boldsymbol{A}$ ． If $\boldsymbol{Y A}=2 t$ and $\boldsymbol{W A}=3 t-4$ ，find $\boldsymbol{Y A}$ ．
$t=$ $\qquad$

EXAMPLE 5：Use parallelogram $A B C D$ to find the indicated values．

$\mathrm{m} \angle \mathrm{AEB}=$ $\qquad$ －
$\mathrm{m} \angle \mathrm{BAD}=$ $\qquad$ ${ }^{\circ}$
$\qquad$。
$\mathrm{m} \angle \mathrm{DCE}=$ $\qquad$
$\mathrm{m} \angle \mathrm{AED}=$ $\qquad$ ${ }^{\circ}$
$\mathrm{m} \angle \mathrm{ADC}=$ $\qquad$。
$\mathrm{m} \angle \mathrm{ECB}=$ $\qquad$ ${ }^{\circ}$
$\mathrm{m} \angle \mathrm{DCB}=$ $\qquad$。

EXAMPLE 6: For each parallelogram, find the values of $\boldsymbol{x}, \boldsymbol{y}$, and $\boldsymbol{z}$.
a.

$X=$ $\qquad$
$y=$ $\qquad$

Z = $\qquad$
b.

$X=$ $\qquad$
$y=$ $\qquad$

Z = $\qquad$


$$
X=
$$

$$
y=
$$

$Z=$ $\qquad$

QUICK CHECK: Find the values of $\mathbf{x}$ and $\mathbf{y}$ to ensure that each quadrilateral is a parallelogram.
a.

b.


$$
\begin{aligned}
& x= \\
& y=
\end{aligned}
$$

